

Passive Microwave Brightness Temperature Assimilation to Improve Snow Mass Estimation across Complex Terrain in Pakistan, Afghanistan, and Tajikistan

Jawairia A. Ahmad, Barton A. Forman, Edward H. Bair, and Sujay V. Kumar

Abstract—An ensemble Kalman filter is used to assimilate Advanced Microwave Scanning Radiometer-2 (AMSR2) observations of passive microwave (PMW) brightness temperatures (spectral differences, ΔT_b) into land surface model estimates of snow mass over northwestern high mountain Asia (HMA). Trained support vector machines (SVMs) serve as the observation operator and map the geophysical modeled variables into ΔT_b space within the assimilation framework. Evaluation of the assimilation routine is carried out through comparison of assimilated snow mass estimates with an in situ dataset. The assimilation framework helps improve the land surface model estimates through PMW ΔT_b assimilation, particularly in terms of decreasing the domain-wide bias. The assimilation framework proved more effective during the (dry) snow accumulation season and decreased the bias and RMSE in snow mass estimates at 76% and 58% of the comparative pixels, respectively. During the snow ablation season, the PMW brightness temperature signal contained less information related to snow mass due to the presence of other concurrent geophysical features that effectively serve as noise during the snow mass update. The utilization of PMW ΔT_b for accurate snow mass estimation in complex terrain such as HMA is dependent on a multitude of factors for optimal results; however, it does add utility to the land surface model if the relevant pitfalls are taken into consideration prior to the state variable update.

Index Terms—passive microwave, brightness temperature, land surface modeling, hydrology, snow, high mountain Asia, NASA Land Information System

I. INTRODUCTION

SNOW water equivalent (SWE) represents the amount of water obtained if the snowpack was converted into liquid water. SWE is an important variable in the context of local and regional hydrology. The equivalent amount of water contained within the snowpack influences runoff in rivers downstream during the snow ablation period. Rivers that originate in the mountain ranges of high mountain Asia (HMA) depend on the snow and glacier melt, to varying degrees, for their runoff [1], [2]. Consequently, the population residing in those river basins depends significantly on the runoff generated [3], [4], which in turn is dependent on the snow and ice melting patterns

J. Ahmad and B. Forman are with the Department of Civil and Environmental Engineering, University of Maryland, College Park, MD, USA (jahmad@umd.edu; baforman@umd.edu)

E. Bair is with the Earth Research Institute, University of California, Santa Barbara, CA, USA (nbair@eri.ucsb.edu)

S. Kumar is with the Hydrological Sciences Laboratory, NASA Goddard Space Flight Center, Greenbelt, MD, USA (sujay.v.kumar@nasa.gov)

upstream. However, there is considerable uncertainty regarding the spatial and temporal variation of snow in HMA. This uncertainty must be minimized in order to better understand the current snow mass (and corresponding runoff) variability and the resulting implications for regional freshwater access.

Various methods, utilizing different ranges of the electromagnetic spectrum, have been used to estimate SWE in the past. SWE estimation algorithms have traditionally used the difference between brightness temperatures observed at lower (e.g., 10.7 or 18.7 GHz) versus higher frequencies (e.g., 36 GHz) to retrieve SWE information [5]. Radiation emitted at a higher frequency from the underlying soil is preferentially scattered by the dry, overlying snowpack as compared to radiation emitted at a lower frequency at the same polarization [6]. Brightness temperature, T_b , is a measure of the radiation emitted by a surface while brightness temperature spectral difference, ΔT_b , is the difference between T_b observed at different frequencies at a given polarization. More specifically, the Raleigh-Jean approximation for microwave radiation defines T_b as the product of emissivity (a dimensionless surface property) and physical temperature of the microwave emitting surface [7]. Satellite-based radiometers observe the brightness temperatures of the underlying surface, which are subsequently used to extract information about relevant geophysical variables such as snow water equivalent [8]. Alternatively, reconstruction methods utilize the snowmelt generated by the snowpack to estimate the total integrated SWE [9]. Molotch and Margulis [10] used a snowmelt simulation model and visible imagery from Landsat Enhanced Thematic Mapper (ETM+), Moderate Resolution Imaging Spectroradiometer (MODIS), and Advanced Very High Resolution Radiometer (AVHRR) to estimate the amount of SWE accumulation. While providing useful information, reconstruction techniques are dependent on the complete melt-out of the snowpack (end of the snow season) before the snow depletion curves can be developed.

Several previous studies have endeavored to estimate SWE in HMA. Kirkham et al. [11] attempted SWE estimation in the Langtang Valley catchment in Nepal by amalgamating numerical modeling techniques with in situ data. Bair et al. [12] attempted SWE prediction in the watersheds of Afghanistan using machine learning algorithms and physiographic predictors. Although encouraging results have been achieved through various schemes at the basin or catchment level [11], [13], there is a need to develop a technique that can be consistently

85 applied over the whole data-scarce HMA domain, including
86 the Hindu Kush and Himalaya mountain ranges in the west and
87 center as well as the monsoon-dominated regions in the center
88 and east of HMA. In this study, we explore the utilization of
89 data assimilation to formulate a consistent technique for SWE
90 estimation over the whole HMA domain.

91 Data assimilation (DA) is the integration of observed data
92 into model estimates. Synthetic experiments carried out by
93 Kwon et al. [14] to study the applicability of PMW ΔT_b
94 assimilation to improve SWE estimation across HMA showed
95 that the assimilation framework was effective in improving
96 SWE estimates for SWE depths < 200 mm during dry
97 snowpack conditions. Building upon these synthetic tests, this
98 study utilizes real-world PMW ΔT_b observations from the
99 Advanced Microwave Scanning Radiometer-2 (AMSR2) in an
100 attempt to improve snow mass estimates across HMA.

II. STUDY DOMAIN

102 High mountain Asia (HMA) is generally defined as the high
103 elevation region within the Asian continent that spans over
104 eight countries—Tajikistan, Afghanistan, Pakistan, India, China,
105 Nepal, Bhutan, and Bangladesh—and three main mountain
106 ranges—Hindu Kush, Karakorum, and Himalaya (Fig. 1).

107 According to the Sturm and Holmgren classification, the
108 snow in HMA is primarily composed of prairie and ephemeral
109 snow types along with the presence of alpine and maritime
110 snow near the glacier zones located at the border between
111 Pakistan and China [15]. Hammond et al. [16] observed that
112 low snow zones coincide with areas of low elevation and
113 that snow persistence increases with elevation. Several studies
114 have analyzed the loss of snow cover and glacier melt under
115 evolving climatic scenarios in this region [17]–[19]. Hetero-
116 geneous trends in seasonal SWE were reported across HMA
117 based on a PMW-based analysis of change in seasonal SWE
118 [20]. Changes in seasonal snow affect the downstream runoff,
119 especially for the Indus Basin [21]. Cryospheric monitoring
120 of this area is as important as it is difficult due to the harsh
121 climate and inaccessibility of the mountainous regions.

122 Remote sensing in HMA is a complex process primarily
123 due to the high spatial variability in elevation, relatively coarse
124 resolution of available satellite data, the relatively consistent
125 presence of clouds, and a general lack of ground-based mea-
126 surements for model validation and evaluation purposes. In
127 such situations, data assimilation (DA) aids in understanding
128 and improving the estimation of the various geophysical
129 variables such as SWE. In this study, the northwestern part
130 of HMA spanning Pakistan, Afghanistan, and Tajikistan is
131 examined. Data assimilation (DA) of PMW ΔT_b is attempted
132 to improve snow mass estimates in this region. Further details
133 regarding the data assimilation framework are provided in
134 Section III, the results of which employ in situ data during
135 evaluation of the DA results.

III. ASSIMILATION FRAMEWORK

A. Land Information System and Noah-MP

136 The NASA Land Information System (LIS) is a high-
137 performance computing framework used for land surface

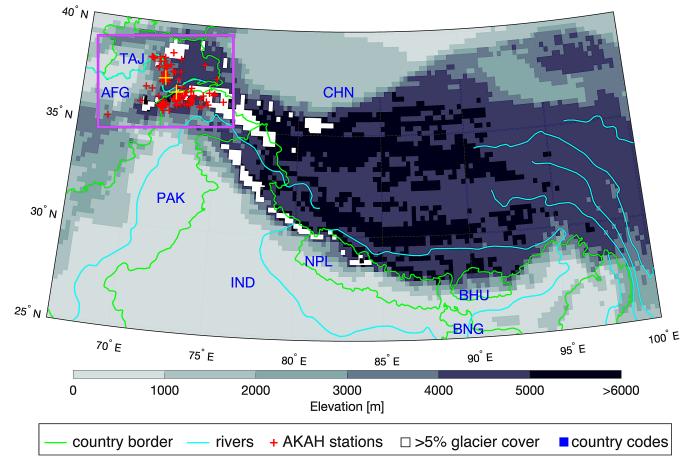


Fig. 1: High mountain Asia comprises multiple countries (country codes in blue text). Glacier cover is computed by up-scaling a binary mask developed using the glacier outlines from the Global Land Ice Measurements from Space (GLIMS) database [22]. The red markers indicate the AKAH stations while the yellow crosses locate the test sites #1 and #2 discussed in Section-V. The purple box demarcates the study domain examined in this study.

140 modeling and data assimilation [23]. The Noah multi-
141 parameterization (MP) version-3.6 [24]–[26] land surface
142 model is run within the LIS version-7.2 framework to model
143 the land surface conditions over northwestern HMA. The
144 multi-layer snowpack modeling approach implemented in
145 Noah-MP provides a reasonable representation of the inter-
146 action between individual snow layers and the geophysical
147 processes inherent in deep snowpacks [25]. Noah-MP sim-
148 ulated geophysical variables were used as input data for support
149 vector machine (SVM) training (Section-III-B) and then as
150 input variables during the prediction of brightness temperature
151 spectral differences using the well-trained SVMs as part of
152 the analysis update aimed at improving the modeled SWE
153 estimates.

154 Table I highlights the Noah-MP parameter options used in
155 this study. The Modern-Era Retrospective analysis for Re-
156 search and Applications Version 2 (MERRA-2) meteorological
157 forcings were used as boundary conditions to Noah-MP [27].
158 The Land Data Toolkit [28] was used to preprocess the
159 ancillary data sets on a 0.25° equidistant cylindrical grid.
160 A spin-up period of 4 years starting in May 2012 and ending in
161 October 2016 helped establish suitable initial conditions for
162 the terrestrial hydrologic cycle.

B. Support Vector Machine Regression

164 Support vector machine (SVM) is a supervised machine
165 learning algorithm developed by Vapnik et al. [39]. In this
166 study, the SVM regression algorithm is used. The SVM
167 framework is composed of two phases: i) training, and ii)
168 prediction. In the *training phase*, known inputs and outputs
169 are used to train support vectors, i.e., define support vectors
170 based on the input data and assign appropriate weights to each
171 support vector [40]. During the *prediction phase*, the trained

| Model Components | Selected Inputs or Parameterizations |
|---|--|
| Elevation, slope, and aspect | SRTM30-v2.0 [29] |
| Landcover | MODIS (IGBP/NCEP) [30] |
| Maximum albedo | National Centers for Environmental Prediction [31] |
| Greenness | National Centers for Environmental Prediction [32] |
| Vegetation | Dynamic vegetation option |
| Canopy stomatal resistance | Ball-Berry method [33] |
| Runoff and groundwater | Simple groundwater model, SIMGM [34] |
| Supercooled liquid water and frozen soil permeability | NY06 [35] |
| Surface-layer drag coefficient | General Monin-Obukhov similarity theory [36] |
| Snow surface albedo | Biosphere-Atmosphere Transfer Scheme [37] |
| Partitioning of rain and snowfall | Jordan91 [38] |
| Snow and soil temperature | Semi-implicit option |
| Lower boundary of soil temperature | Noah native option |
| Meteorological boundary conditions | MERRA-2 [27] |

TABLE I: Selection of model components in Noah-MP as implemented within LIS.

| SVM input data | | | |
|---|--------------------------|-------------------|--|
| Noah-MP modeled geophysical variable | Symbol | Unit | |
| Snow water equivalent | SWE | dm | |
| Snow density | ρ_{snow} | dg/m ³ | |
| Snow liquid water content | SLWC | mm | |
| Top-layer snow temperature | ST | cK | |
| SVM target data | | | |
| Tb spectral difference (frequency and polarization) | Symbol | Unit | |
| Tb _{10.7GHz} , vert. pol. - Tb _{36.5GHz} , vert. pol. | ΔT_b 10.7V-36.5V | K | |
| Tb _{10.7GHz} , horz. pol. - Tb _{36.5GHz} , horz. pol. | ΔT_b 10.7H-36.5H | K | |
| Tb _{18.7GHz} , vert. pol. - Tb _{36.5GHz} , vert. pol. | ΔT_b 18.7V-36.5V | K | |
| Tb _{18.7GHz} , horz. pol. - Tb _{36.5GHz} , horz. pol. | ΔT_b 18.7H-36.5H | K | |

TABLE II: List of SVM input and target training data. Separate SVMs are trained to predict each of the individual ΔT_b combinations.

172 SVMs are then used to predict ΔT_b using independent input
173 data.

174 Machine learning techniques such as SVM regression have
175 a unique advantage over regular regression and radiative
176 transfer modeling, i.e., these techniques do not require the
177 explicit representation of each background process via state
178 variables. With respect to radiative transfer models (RTMs)
179 more specifically, RTMs often require inputs that global land
180 surface models cannot provide. That is, global land surface
181 models often lack the fidelity as required by the RTMs,

182 hence, SVM regression provides an alternative approach that
183 enables the use of all of the available information (e.g., soils
184 information, vegetation information) beyond that provided by
185 the snow model and corresponding snow model states. In
186 other words, the input and target data space employed by
187 the SVM regression algorithm does not require the explicit
188 modeling or inclusion of each individual state and parameter
189 [41]. Compared to linear regression techniques, SVM is able
190 to represent the non-linear complexity within the relationship
191 between the input and target data that linear regression
192 techniques cannot. Furthermore, a comparative study of SVM
193 and artificial neural network (ANN) predictions of brightness
194 temperature showed that the SVM outperformed the ANN by
195 capturing more of the high-frequency variability, and in turn,
196 exhibiting a lower RMSE and a higher anomaly correlation
197 coefficient. For places such as HMA, where previous (accu-
198 rate) knowledge of snow mass is limited, SVM regression
199 serves as a reasonable modeling technique that maps the
200 geophysical states into the ΔT_b space. However, some, but
201 not all, of the relevant processes (and state variables) are
202 implicitly represented through each trained SVM based on
203 the relationship between the input and target data. The fidelity
204 provided by machine learning algorithms make them suitable
205 for use in areas where information about each state variable is
206 lacking. In addition, the SVMs trained at each pixel implicitly
207 represent the local spatiotemporal features such as topography
208 and regional climatology.

209 Table II presents the SVM input and target data specifi-
210 cations. Based on their sensitivity to ΔT_b [42], four Noah-
211 MP modeled geophysical variables (SWE, snow liquid wa-
212 ter content, snow density, and top-layer snow temperature)
213 were selected and used as input data for SVM training and
214 prediction. All the Noah-MP variables were converted into
215 units with similar orders of magnitude in order to better
216 produce appropriate SV weights (third column in Table II).
217 The rescaling via simple unit conversion helps to maintain
218 better consistency between all of the SVM input signals
219 relevant to PMW remote sensing of snow.

220 The SVM training targets consisted of four different
221 frequency-polarization combinations of the PMW T_b observed
222 by Advanced Microwave Scanning Radiometer-EOS (AMSR-
223 E). PMW T_b observed by the AMSR-E instrument at three
224 different frequencies (i.e., 10.7 GHz, 18.7 GHz, and 36.5
225 GHz) and two polarizations (horizontal and vertical) were
226 used, Table II. These ΔT_b combinations have been used in
227 numerous studies for SWE estimation [8] [14] [43]. AMSR-E
228 provides T_b observations from 2002-2011 while the AMSR2
229 T_b observations are available from 2012-present. SVMs were
230 trained using AMSR-E ΔT_b while the AMSR2 ΔT_b were
231 assimilated during the DA run. Transferability from AMSR-
232 E to AMSR2 ΔT_b was analyzed (results not shown here)
233 and it was concluded that the AMSR-E ΔT_b trained SVMs
234 were able to predict the AMSR2 ΔT_b climatology. The use
235 of AMSR-E ΔT_b for training and AMSR2 ΔT_b for prediction
236 also provides the necessary independence between the training
237 and prediction datasets.

238 Fig. 2(a-f) presents the AMSR2 observed T_b s at relevant
239 frequencies and polarizations for one day during the snow

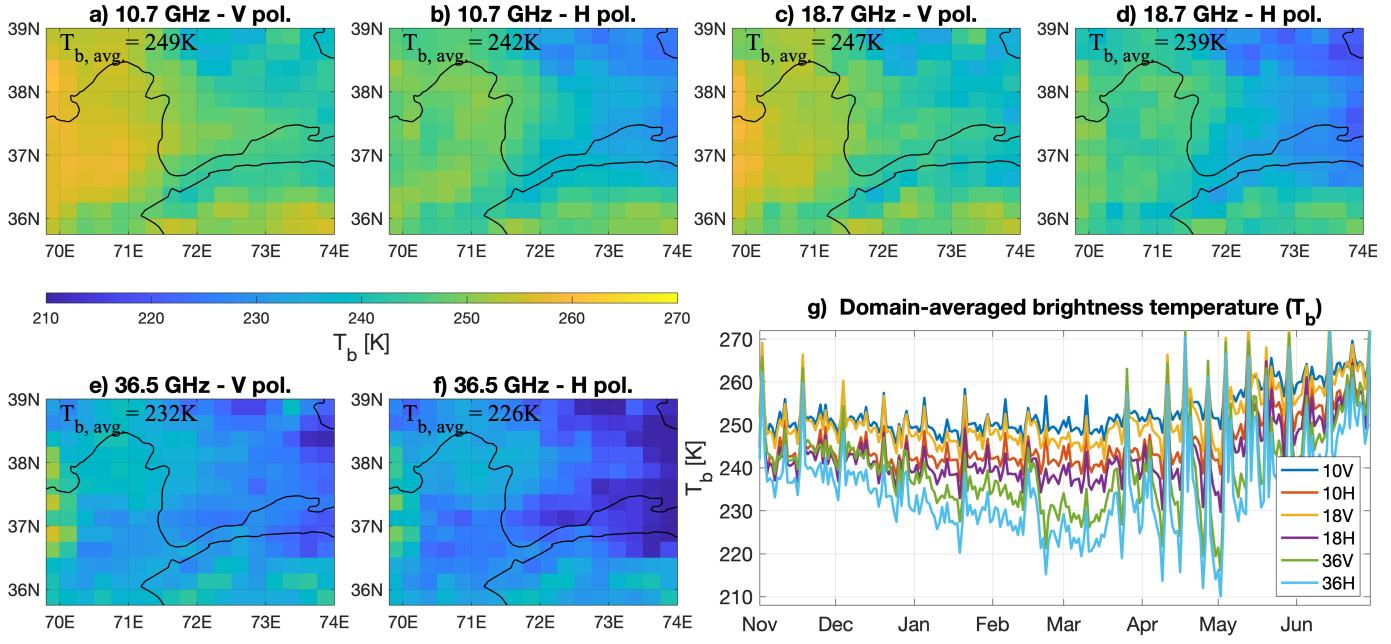


Fig. 2: AMSR2 observed brightness temperatures (T_b) at various frequencies and polarizations across the Pakistan-Afghanistan-Tajikistan sub-domain for February 11, 2017. Subplot (a-f) titles identify the microwave frequency and polarization of the corresponding T_b maps. Subplot g) displays the temporal variation of domain-averaged T_b values for the 2017 snow season. Large differences between the T_b s observed at lower (10.7 and 18.7 GHz) vs. higher (36.5 GHz) frequencies suggest the presence of snow across the area.

240 season (February 11, 2017). Relatively higher T_b magnitudes
 241 were observed across the western part of the sub-domain,
 242 which gradually decreased to much lower magnitudes towards
 243 the northeast. The differences between the T_b s observed at
 244 the lower frequencies (10.7 and 18.7 GHz) versus the higher
 245 frequency (36.5 GHz), known as spectral differences, indicate
 246 the presence of snow across the region. Fig. 2h displays
 247 the seasonal variation in the observed T_b s and highlights
 248 the increase in the spectral differences during the snow
 249 accumulation months and the subsequent decrease in these
 250 differences during the ablation months. Interesting to note is
 251 the corresponding increase in the T_b temporal variations (for
 252 all frequencies) during the ablation months (April onwards).
 253 Only PMW T_b s observed during the nighttime overpass
 254 were assimilated to minimize the influence of wet snow
 255 conditions. Wet snow not only attenuates the PMW emitted
 256 from the Earth's surface but also emits significant PMW
 257 radiation itself, as compared to dry snow, thus leading to
 258 an increased T_b magnitude observed by the radiometer and
 259 possible erroneous estimation of snow [44]. AMSR-E and
 260 AMSR2 T_b observations were downloaded from the Japan
 261 Aerospace Exploration Agency GCOM website (URL:https://suzaku.eorc.jaxa.jp/GCOM_W/data.html)
 262 and mapped to the same 0.25° equidistant cylindrical grid as
 263 used by Noah-MP in order to maintain spatial coherence.
 264 Further details regarding the SVM theory and training setup
 265 are provided in Section-A1.

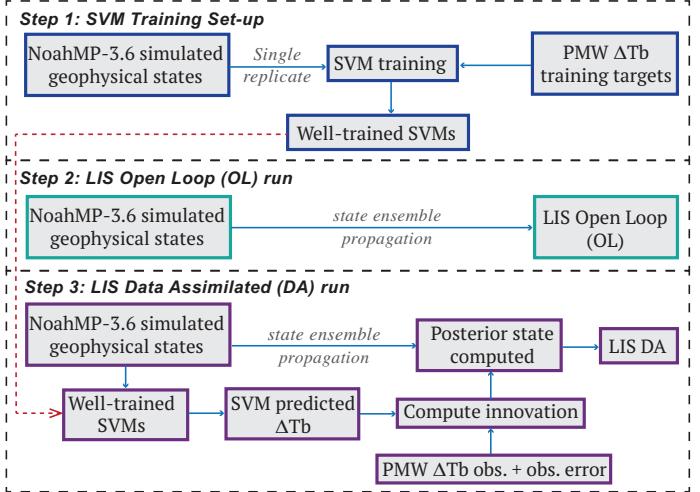


Fig. 3: Three-step approach for the data assimilation experimentation including SVM training, LIS open loop (OL), and LIS data assimilation.

C. Open Loop and Data Assimilation Setup

268 Fig. 3 illustrates the SVM training, open loop (OL), and
 269 data assimilation (DA) experiments. The experiments begin
 270 with an open loop (OL) simulation, which is defined as
 271 the *model-only* run. Stochastic state and boundary condition
 272 (forcing) perturbations are applied to develop an appropriate
 273 state ensemble, after which the ensemble replicates are

274 independently propagated in time using the forward model
 275 (i.e., Noah-MP). Forcing perturbation characterizations are the
 276 same as those detailed in Table 2 by Kwon et al. [14]. The
 277 prognostic state variables (SWE and snow depth) are also per-
 278 turbed to represent the model structure error via multiplicative
 279 perturbations. The ensemble spread implicitly represents the
 280 uncertainty in the model predictions due to model structure
 281 error and error in the boundary conditions. The OL serves as
 282 the benchmark for model-only performance without the benefit
 283 of information derived from satellite-observed PMW ΔT_b .
 284 The OL and DA runs are propagated through a 20-member
 285 ensemble. Since a one-dimensional assimilation framework is
 286 used in this study, spatial error correlations were not explicitly
 287 considered. However, the general framework outlined here
 288 could be expanded to include spatially-correlated errors as part
 289 of a follow-on study, but are excluded here in order to maintain
 290 a tractable project scope.

291 The Ensemble Kalman Filter (EnKF) data assimilation
 292 algorithm is utilized to assimilate ΔT_b in this study. The DA
 293 simulation has two main steps: i) state propagation, and ii)
 294 state update. The ensemble development and propagation is
 295 similar to the OL, however, the update step requires computa-
 296 tion of both the Kalman gain and the innovation by comparing
 297 the SVM-based predictions of ΔT_b versus the observed ΔT_b .
 298 The ensemble replicate update in the EnKF is computed as:

$$y_{i,t}^+ = y_{i,t}^- + K_t \text{Innov}_{i,t} \quad (1)$$

$$K_t = C_{y_t z_t} [C_{z_t z_t} + C_{vv}]^{-1} \quad (2)$$

$$\text{Innov}_{i,t} = z_t + v_{i,t} - \mathcal{H}(y_{i,t}^-) \quad (3)$$

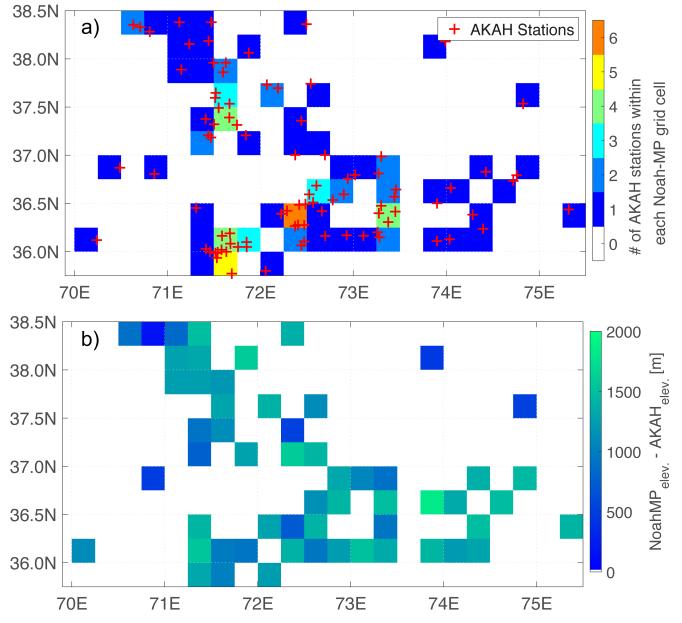
299 such that i = index of the replicate drawn from a derived
 300 probability distribution of size N ; $y_{i,t}^+$ = posterior SWE value
 301 of replicate i at time t ; $y_{i,t}^-$ = prior SWE estimate of replicate i
 302 at time t ; K_t = Kalman gain at time t ; z_t = observation at time
 303 t ; $v_{i,t}$ = observation error at time t ($v_{i,t} \sim \mathcal{N}(0, \sigma_{vv}^2)$); $\mathcal{H}(\cdot)$ is
 304 the non-linear observation operator that maps the geophysical
 305 state space into the corresponding observation (ΔT_b) space;
 306 $C_{y_t z_t}$ = time-varying cross-covariance matrix between the prior
 307 state errors and the predicted observation errors; $C_{z_t z_t}$ =
 308 time-varying predicted observation error covariance matrix;
 309 C_{vv} = time-invariant observation error covariance matrix; and
 310 $\text{Innov}_{i,t}$ = innovation vector for replicate i at time t . In the
 311 EnKF, $C_{y_t z_t}$ and $C_{z_t z_t}$ are approximated from the ensemble
 312 sample statistics using the following formulas:

$$C_{y_t z_t} = E[(y_t^- - \bar{y}_t^-)(z_{\text{pred}_t} - \bar{z}_{\text{pred}_t})^T] \quad (4)$$

$$C_{z_t z_t} = E[(z_{\text{pred}_t} - \bar{z}_{\text{pred}_t})(z_{\text{pred}_t} - \bar{z}_{\text{pred}_t})^T] \quad (5)$$

313 where $E[\cdot]$ = expectation operator, \bar{y}_t^- =
 314 $\{y_{1,t}^-, \dots, y_{i,t}^-, \dots, y_{N,t}^-\}$; \bar{y}_t^- = temporal mean of y_t^- ; z_{pred_t} =
 315 $\{z_{\text{pred}_{1,t}}, \dots, z_{\text{pred}_{i,t}}, \dots, z_{\text{pred}_{N,t}}\}$; $z_{\text{pred}_{i,t}}= \mathcal{H}(y_{i,t}^-)$; and
 316 \bar{z}_{pred_t} = temporal mean of z_{pred_t} .

317 The EnKF has certain inherent assumptions: i) unbiased,
 318 linear forward model, ii) unbiased, linear observation operator,
 319 iii) jointly Gaussian and mutually independent observation
 320 and model errors, and iv) spatiotemporally uncorrelated errors.
 321 However, the EnKF provides certain flexibility such that suc-



322 Fig. 4: a) Map of the number of AKAH stations within each
 323 Noah-MP grid cell. b) Visual representation of the difference
 324 between the Noah-MP grid cell elevation and the average elevation
 325 of AKAH stations within the grid cell boundary. AKAH
 326 stations within each grid cell are averaged for comparison with
 327 the corresponding Noah-MP cell.

328 cessful results have been observed for non-linear models and
 329 observation operators [14], [43]. Exploiting this flexibility, a
 330 non-linear forward model (Noah-MP) and observation operator
 331 (SVM) are utilized here.

IV. EXPERIMENTAL SETUP

A. Evaluation Data

332 Evaluation of the OL and DA results was predicated on the
 333 use of in situ snow depth measurements (details in Section-
 334 IV-A1). However, due to a lack of temporally-consistent SWE
 335 measurements, the in situ snow depth measurements were used
 336 as boundary conditions in a separate and independent snow
 337 model (SNOWPACK) in order to derive SWE estimates at the
 338 station locations (details in Section-IV-A2). SNOWPACK was
 339 used to provide temporally-consistent and gap-free timeseries
 340 of SWE that could be used as a reasonable proxy for in situ
 341 SWE measurements.

342 1) AKAH Snow Depth: The Aga Khan Agency for Habitat
 343 (AKAH) provided in situ snow depth measurements from 93
 344 stations within Tajikistan, Afghanistan, and Pakistan, Fig. 1
 345 and Fig. 4. The in situ measurements were collected at the
 346 point-scale whereas the Noah-MP grid size was $0.25^\circ \times 0.25^\circ$
 347 ($\sim 25\text{km} \times 25\text{km}$ at mid-latitudes).

348 Fig. 4a presents the location and number of stations per
 349 Noah-MP grid cell. Some grid cells contain multiple AKAH
 350 stations within the same elevation range. However, several
 351 grid cells contain stations which have large elevation differ-
 352 ences. For consistency, an average of the station (point-scale)
 353 snow depth measurements was computed, wherever applicable,

| Type | Update frequency | Assimilation period | Assimilated observations | States used in evaluation |
|----------------------------------|---------------------------|---------------------|--------------------------|---------------------------|
| Standard assimilation | ~ daily | Nov 1- Jun 30 | AMSR2 ΔT_b | Snow depth, SWE |
| Data thinning-based assimilation | every 5 th day | Nov 1- Jun 30 | AMSR2 ΔT_b | Snow depth, SWE |
| Seasonal assimilation | ~ daily | Nov 1- Mar 22 | AMSR2 ΔT_b | Snow depth, SWE |

TABLE III: Summary of the LIS-NoahMP assimilation runs described in Section-IV-B.

350 to compare against the Noah-MP (model-scale) snow depth
 351 estimates. For those cells that contained only one station,
 352 the station measurements were used directly in comparisons
 353 against the model grid cell.

354 Fig. 4b highlights the difference between the AKAH station
 355 elevations and the corresponding Noah-MP grid cell elevations.
 356 The AKAH stations have lower average elevation values
 357 compared to their corresponding Noah-MP grid cells. The
 358 ground stations are generally located at lower elevations (i.e.,
 359 closer to population) for ease of management and maintenance
 360 rather than at the mountain peaks. It is, therefore, acknowled-
 361 ged that the discrepancy in ground station versus grid cell
 362 elevation can lead to a potential positive bias in the Noah-MP
 363 snow depth estimates.

364 2) *SNOWPACK SWE*: SNOWPACK is an open source snow
 365 and land surface model focusing on the mass and energy
 366 exchange between snow and the atmosphere [45], [46]. Mainly
 367 used for avalanche studies, here it is used to model the SWE
 368 based on the AKAH snow depth values along with ancillary,
 369 downscaled boundary conditions. Due to a dearth of any con-
 370 sistent SWE dataset available in this region, the SNOWPACK
 371 model estimates of SWE derived from the AKAH snow depth
 372 measurements are assumed to be representative of the ground
 373 conditions and are, therefore, utilized in the evaluation of the
 374 OL and DA SWE estimates. Previous analysis of SNOWPACK
 375 modeled SWE (over Mammoth Mountain, U.S.A.) showed
 376 encouraging results relative to in situ SWE measurements
 377 when using snow depth (not total precipitation) as the model
 378 boundary condition [47]. The quality of the SNOWPACK
 379 SWE derived from in situ snow depth measurements used
 380 in this study is, however, expected to be less than the SWE
 381 modeled using SNOWPACK for Mammoth Mountain, U.S.A
 382 by [47]. It is expected that there can be some loss of accuracy
 383 as the snow depth measurements are translated into SWE using
 384 ancillary data (i.e., downscaled meteorological forcings). In
 385 Bair et al. [47], all the energy balance forcings, especially
 386 the radiative fluxes and snow albedo, were measured on site.
 387 For the AKAH snow depth, on the other hand, downscaled
 388 Global Land Data Assimilation System (GLDAS-2, [48]) and
 389 Clouds and Earth Radiant Energy System (CERES, [49]) data
 390 are used, which can introduce additional error and uncertainty.

391 The SNOWPACK model forces the modeled snow ac-
 392 cumulation to match the in situ snow depth measurements
 393 during the accumulation period, while during the ablation
 394 period the modeled snow ablation is not updated to match
 395 the measured snow depth. Therefore, given reliable daily
 396 snow depth measurements, modeled SWE during the snow
 397 accumulation season is expected to contain less uncertainty
 398 and be closer to the in situ ground measurements, while

399 during the snow ablation season the uncertainty and error
 400 likely increases. Comparing the SNOWPACK and AKAH
 401 snow depths, the average bias and RMSE were noted to be 4.4
 402 cm and 9.7 cm, respectively. These values are much smaller
 403 relative to the average bias and RMSE computed for the Noah-
 404 MP OL and DA snow depth estimates (see Table IV). Since
 405 daily snow depth data are utilized as boundary conditions to
 406 SNOWPACK, AKAH stations that had nearly continuous daily
 407 snow depth measurements recorded were selected, i.e., only
 408 those stations where greater than 80% of the days in the snow
 409 season (Nov-May) had snow depth measurements recorded
 410 were used. Therefore, the number of stations included in the
 411 SWE evaluation (Section-V-B) is only 52 as compared to the
 412 93 stations used to evaluate snow depth estimates. Further
 413 details regarding the SNOWPACK model parameter selection
 414 and ancillary forcing inputs is provided in Appendix-A3.

B. Types of assimilation runs

415 Three different types of assimilation runs were conducted:
 416 i) standard assimilation, ii) data thinning-based assimilation,
 417 and iii) seasonal assimilation (Table III). All of the DA
 418 estimates shown here use $\sigma_{vv} = 3$ K for the ΔT_b observation
 419 error standard deviation. Details of, and motivation for, each
 420 assimilation run are provided below.

421 1) *Standard assimilation*: The standard assimilation run
 422 consists of near-daily (based on AMSR2 overpass frequency)
 423 ΔT_b assimilation into the Noah-MP SWE estimates using
 424 Equations 1, 2, and 3. This is the standard EnKF implemen-
 425 tation run without any modifications.

426 2) *Data thinning-based assimilation*: The standard EnKF
 427 algorithm does not take rational constraints related to physical
 428 processes into account during the update process. For example,
 429 it is not likely that a snowpack will melt 100 cm overnight,
 430 however, if the ΔT_b observation suggests a 100 cm decrease
 431 in snow depth, the computed innovation could result in a
 432 sudden and deleterious decrease in the updated snow depth
 433 and SWE. Given such a scenario, it is likely that noise
 434 or information relevant to other physical features (e.g., soil
 435 moisture) in the satellite ΔT_b observations could result in
 436 unrealistic snow mass updates. Fig. 5 displays the presence of
 437 high frequency noise in the PMW ΔT_b signal, which provides
 438 the motivation for conducting data thinning experiments as a
 439 means of mitigating some of this noise. The high-frequency
 440 variability is categorized as "noise" here in terms of SWE
 441 only, i.e., it is related to information in the ΔT_b signal that is
 442 not relevant to SWE. It does not necessarily represent sensor
 443 noise per se. Rather, this is information that masks the snow
 444 mass signal that is required for SWE estimation, hence, it acts
 445 as noise in terms of SWE estimation specifically. This signal

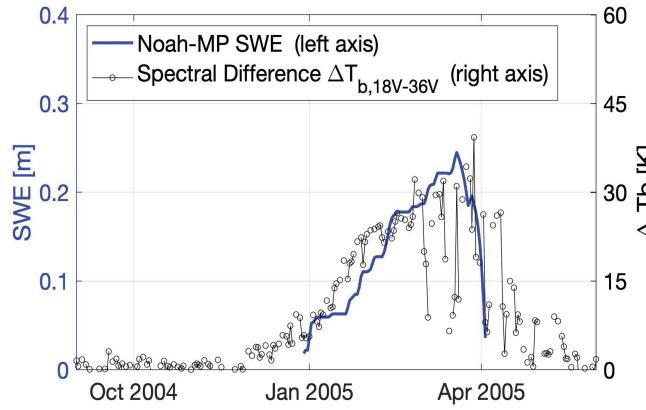


Fig. 5: Modeled SWE estimates via Noah-MP as compared to ΔT_b observations collocated at a point in the HMA study domain. High frequency noise in the PMW ΔT_b observations is translated into noise in the subsequently calculated a posteriori SWE estimate.

447 is due to multiple, concurrent processes. The presence of wet
448 snow or even ice layers within the snowpack would affect the
449 electromagnetic response of the snowpack by changing the
450 scattering response of the snow layers [50].

451 Data thinning is attempted to minimize the occurrence of
452 irrational snow mass updates associated with noise or snow
453 mass-irrelevant information in the ΔT_b observations. Data
454 thinning consists of paring down the available observations
455 such that the assimilation occurs over incremental days. By de-
456 creasing the number of assimilation occurrences, it is expected
457 that: i) the possibility of the assimilation of high frequency
458 observation noise into the model estimates will decrease, and
459 ii) the resultant snow depth and SWE timeseries will exhibit
460 a smoother snowpack accumulation and ablation as compared
461 to standard assimilation. An increment of five days was used
462 here such that ΔT_b assimilation occurred on every fifth day.
463 The incremental value was selected based on results yielded
464 by synthetic data thinning experiments carried out by Wang et
465 al. [51] which suggested that an increment of 3-5 days yielded
466 the best results.

467 3) *Seasonal assimilation*: Estimation of SWE from PMW
468 radiometry in the presence of wet snow is a complex, ill-posed
469 problem. The influence of wet snow on the PMW radiation
470 emitted from the underlying ground is different as compared
471 to dry snow [52]. The dielectric constant of wet snow is
472 significantly larger than dry snow due to the presence of liquid
473 water within the snowpack. Thus, wet snow not only attenuates
474 the PMW radiation emitted by the underlying ground but also
475 emits its own microwave radiation [44]. The emissivity of dry
476 versus wet snow is significantly different [50]. Therefore, the
477 relationship between SWE and ΔT_b varies for dry versus wet
478 snowpacks [5]. These differences render it difficult to extract
479 only SWE-relevant information from the observed T_b during
480 the (wet) snow ablation period.

481 The influence of wet snow on the PMW radiation emitted
482 from the underlying ground is different as compared to dry
483 snow. The dielectric constant of wet snow is higher than dry

484 snow due to the presence of liquid water within the snowpack.
485 Thus, wet snow not only attenuates the PMW radiation emitted
486 by the underlying ground but also emits its own microwave
487 radiation [44]. This phenomenon renders it difficult to extract
488 only SWE-relevant information from the observed ΔT_b . Kwon
489 et al. [14] found that SVM-based ΔT_b prediction efficacy
490 was reduced in the presence of snow liquid water content. To
491 overcome this issue, the effect of disabling the assimilation
492 update during significant snow melt (ablation period) was
493 analyzed.

494 The AKAH stations also provide in situ rainfall data, which
495 was leveraged to better determine a date on which to cease the
496 daily ΔT_b assimilation as part of the seasonal assimilation
497 experiment. The winter rainfall began in March for most
498 of the AKAH stations. The date of occurrence of the first
499 rainfall greater than 5 mm/day for each station was noted. The
500 average (station) median date for snow seasons from 2016 to
501 2020 was 22 March. Snow cover fraction from the Interactive
502 Multisensor Snow and Ice Mapping System (IMS) snow cover
503 product [53] was also employed as a secondary check. By 22
504 March, the domain had passed the point of maximum snow-
505 covered area ($\sim 30\%$ of total domain area covered with snow)
506 and had entered the ablation period ($\sim 17\%$ of total domain
507 area still covered with snow). A seasonal run was therefore
508 conducted with standard assimilation until 22 March, after
509 which assimilation was disabled and the model was run in the
510 OL (model-only simulation) configuration. Here we are using
511 a first-order approach to identify the general transition from
512 solid to liquid precipitation (thus indicating a high probability
513 of wet snowpack conditions across the HMA domain).

V. RESULTS

514 The evaluation results are separated into two parts. In the
515 first part, AKAH snow depth is the geophysical variable used
516 to evaluate the accuracy of the OL versus DA estimates. In the
517 second part, SNOWPACK modeled SWE is used to evaluate
518 the OL and DA SWE estimates. Fig. 4a details the number
519 of AKAH stations within each Noah-MP grid cell used for
520 comparison.

A. Snow depth evaluation

522 1) *Standard Assimilation*: The two timeseries in Fig. 6a
523 illustrate the differences between the OL and DA snow depth
524 estimates as compared to the in situ measurements at two test
525 locations (test site locations marked in Fig. 1). For test site #1,
526 the assimilation generally improves the snow depth estimates
527 up until the snow ablation period when the assimilation visibly
528 degrades the predicted estimates, especially during Apr and
529 May, as high frequency noise (in the context of snow mass)
530 present in the AMSR2 ΔT_b signal is assimilated into the
531 modeled snow depth. During the dry snow accumulation
532 months (generally Nov-Feb), the DA estimates are better
533 encapsulated by the standard deviation of the in situ snow depth
534 measurements at stations located within the test grid cell as
535 compared to the OL. Fig. 6a also highlights the presence of a
536 general temporal offset in the snowpack development between
537 the Noah-MP OL simulation and the ground measurements.

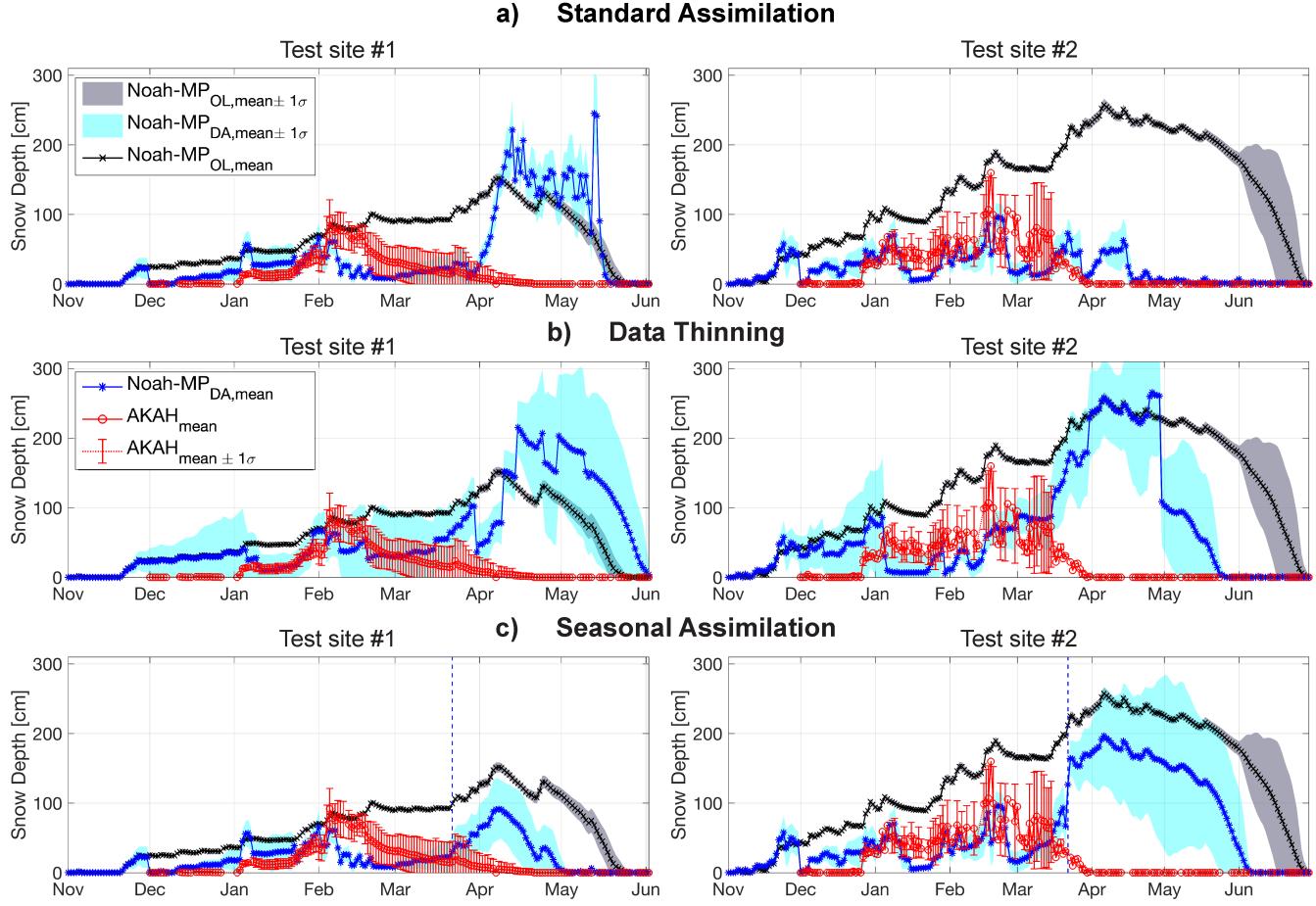


Fig. 6: Comparative timeseries of OL and DA snow depth estimates vs. AKAH measured snow depth for the 2016-2017 snow season. The dashed lines in part c) locate the date (22 March) when assimilation is disabled for seasonal assimilation. The red solid line represents the mean while the red whiskers represent the standard deviation calculated from AKAH station measurements that lie within the Noah-MP grid cell.

539 The OL model simulation peak occurs in Apr as compared to
 540 Feb for the ground stations. For test site #2, ΔT_b assimilation
 541 updates and improves the complete melt-out date.

542 Timeseries for both test sites highlight the increase in
 543 uncertainty after assimilation as compared to the OL. The
 544 OL ensemble exhibits a restricted dynamic range (ensemble
 545 spread) as compared to the DA ensemble estimates. However,
 546 the OL ensemble uncertainty increases during the snowpack
 547 ablation period. In general, the DA ensemble estimates better
 548 encapsulate the AKAH snow depth measurements, especially
 549 from Nov-Mar. The increased ensemble uncertainty is apparent
 550 in all the DA experiments, i.e., standard assimilation, data
 551 thinning, and seasonal assimilation. Therefore, it can be stated
 552 that assimilating the PMW ΔT_b observations increases the
 553 ensemble uncertainty as the snow mass-related ΔT_b uncer-
 554 tainty is also integrated into the model estimated snow depth
 555 uncertainty.

556 2) *Data thinning-based assimilation*: In Fig. 6b, the time-
 557 series for test sites #1 and #2 exhibit relatively consistent snow
 558 depth changes until the advent of the ablation period. Similar
 559 to the standard assimilation run (Fig. 6a test site #1), the snow
 560 depth estimates are visibly degraded by assimilation during

561 the snow ablation period. The uncertainty represented by the
 562 ensemble spread is much larger for both test sites than for
 563 standard assimilation. Observing the two test site timeseries,
 564 the data thinning approach yielded smooth sections of the
 565 timeseries that underwent sudden, large updates rendering the
 566 snowpack development more discontinuous as compared to the
 567 standard assimilation results.

568 3) *Seasonal assimilation*: The timeseries for test site #1 in
 569 Fig. 6a and Fig. 6b showed that the assimilated values and the
 570 ground measurements diverge significantly during the snow
 571 ablation months. In Fig. 6c, degradation via assimilation is
 572 avoided as the assimilation is disabled after 22 March 2017.
 573 This also results in a reduced off-set between the ground
 574 station measured and the DA predicted snowpack melt-out
 575 dates. However, for test site #2, disabling assimilation after
 576 22 March 2017 also results in: i) no opportunity to correct the
 577 model estimate through an update (based on ΔT_b assimilation)
 578 and ii) an increase in the ensemble uncertainty in a manner
 579 similar to the data thinning run. Fig. 6 highlights the location
 580 specificity of the test sites' response to the three different
 581 assimilation methods. Response of the test grid cells to the
 582 three different assimilation approaches varies from location to

583 location.

| Statistic [cm] | Open Loop | Standard Assimilation | Data Thinning | Seasonal Assimilation |
|----------------------|-----------|-----------------------|---------------|-----------------------|
| Mean Bias | 75.4 | 45.7 | 63.3 | 48.6 |
| Median Bias | 76.5 | 32.6 | 47.5 | 42.3 |
| Mean RMSE | 91.4 | 76.5 | 89.4 | 74.2 |
| Median RMSE | 86.2 | 64.6 | 74.6 | 63.4 |
| Mean Unbiased RMSE | 49.9 | 57.6 | 59.1 | 52.4 |
| Median Unbiased RMSE | 50.7 | 48.6 | 57.4 | 45.5 |

TABLE IV: Domain-average and domain-median of bias, RMSE, and unbiased RMSE for OL and DA snow depth estimates as compared to the AKAH snow depth measurements for the 2016-17 snow season. All values are in units of centimeter.

584 *4) Statistical results:* Statistics in Table IV are computed
 585 using the average snow depth of the stations within each
 586 grid cell, thus the total number of cells used for calculation
 587 is equal to 55. The smallest domain-averaged bias occurs
 588 in the standard assimilation snow depth estimates while the
 589 smallest domain-averaged RMSE is observed for the standard
 590 and seasonal assimilation runs. The domain-median values
 591 similarly show better performance for the standard assimilation
 592 runs relative to the other simulations. The domain-averaged
 593 bias and RMSE for the data thinning run are much larger than
 594 either the standard or seasonal assimilation runs, Table IV.
 595 However, all three assimilation runs yield better domain-wide
 596 statistical results as compared to the OL, Table IV.

597 The computed statistics were further analyzed with respect
 598 to land cover type and elevation. It was found that the
 599 average bias in snow depth estimates for pixels categorized
 600 as barren land cover was relatively lower for standard and
 601 seasonal assimilation runs (36 cm and 41.5 cm respectively) as
 602 compared to the OL and data thinning runs (79 cm and 67 cm
 603 respectively). Correlations calculated between pixel elevations
 604 and statistics (bias and RMSE) were all; i) negative (i.e., as
 605 elevation increases the snow depth estimates improve), and ii)
 606 $|R| < 0.5$ in magnitude.

607 Table V highlights the influence of assimilation on pixels
 608 within different elevation ranges. Standard assimilation ex-
 609 hibits the lowest mean bias for both elevation ranges and the
 610 lowest mean RMSE for elevation >4000 m. Standard assimila-
 611 tion seems relatively more effective for pixels at elevations
 612 <4000 m. The mean bias is reduced from 88.8 cm to 52.2 cm
 613 (reduction of 36.6 cm) while the mean RMSE is decreased
 614 by 18.5 cm through standard assimilation as compared to the
 615 OL. For elevations >4000 m, where deep snow is expected,
 616 the difference between the various runs is relatively reduced.
 617 The maximum reduction in mean bias is equal to 22.4 cm
 618 while the maximum reduction in mean RMSE is equal to 11
 619 cm only. According to the results in Table V, ΔT_b assimilation

| Run Type | Snow depth | | | |
|-----------------------|-----------------------------|----------------|---------------|------------|
| | Elevation of Noah-MP pixels | | | |
| | Mean Bias [cm] | Mean RMSE [cm] | ≤ 4000 m | > 4000 m |
| Open Loop | 88.8 | 61.5 | 105.3 | 76.9 |
| Standard Assimilation | 52.2 | 39.1 | 86.8 | 65.9 |
| Data Thinning | 75.5 | 50.6 | 102.3 | 76.0 |
| Seasonal Assimilation | 54.2 | 42.8 | 80.9 | 67.3 |

TABLE V: Influence of elevation on ΔT_b assimilation performance. The number of pixels with elevation ≤ 4000 m = 28 whereas the number of pixels with elevation > 4000 m = 27.

exhibits greater utility at elevations below 4000 m, specifically
 620 in reducing the bias in modeled estimates.

B. SWE evaluation

Fig. 7 displays the OL and DA SWE estimates for two test
 623 sites. The test sites #1 and #2 included in Fig. 7 are the same
 624 as those presented in Fig. 6. The number of grid cells included
 625 for SWE analysis in this section equals 38 based on the 55
 626 station locations where some grid cells contain more than one
 627 AKAH station.

1) *Standard assimilation:* The DA SWE estimates (Fig. 7a)
 629 resemble the snow depth timeseries (Fig. 6) with better DA
 630 and SNOWPACK-derived SWE conformity (relative to the
 631 open loop) during the snow accumulation period, especially
 632 for test site #1. For test site #2, the complete melt-off date
 633 occurs earlier than the OL snowpack melt-off and is closer to
 634 the SNOWPACK-derived SWE estimates. For test site #1, the
 635 large DA SWE updates during Apr and May appear erroneous
 636 as the SWE values change ~ 50 cm overnight. These large
 637 updates are a consequence of the ill-posed nature of PMW
 638 remote sensing of snow when the snowpack is wet coupled with
 639 controllability issues in the SVM-based observation operators
 640 in the presence of snow liquid water content [14].

2) *Data thinning-based assimilation:* The saw-tooth pattern
 642 and the incorporation of high frequency noise (information
 643 not related to snow mass) motivates the exploration of data
 644 thinning. Fig. 7b shows the effect of data thinning on DA
 645 SWE estimates. Test sites #1 and #2 exhibit a similar temporal
 646 pattern in terms of better consistency with SNOWPACK SWE
 647 during the snow accumulation period and large SWE updates
 648 during the ablation period. The corresponding ensemble un-
 649 certainty is also visibly increased during Apr and May. Similar
 650 to the snow depth timeseries (Fig. 6b), the data thinning
 651 experiment yields SWE estimates that exhibit a temporal
 652 pattern of smooth snowpack development for short intervals
 653 with visible SWE updates via assimilation on incremental
 654 days.

3) *Seasonal assimilation:* Test site #1 in Fig. 7c shows
 655 improved results for the seasonal assimilation run as the
 656 snowpack melt-off date more closely agrees with SNOWPACK

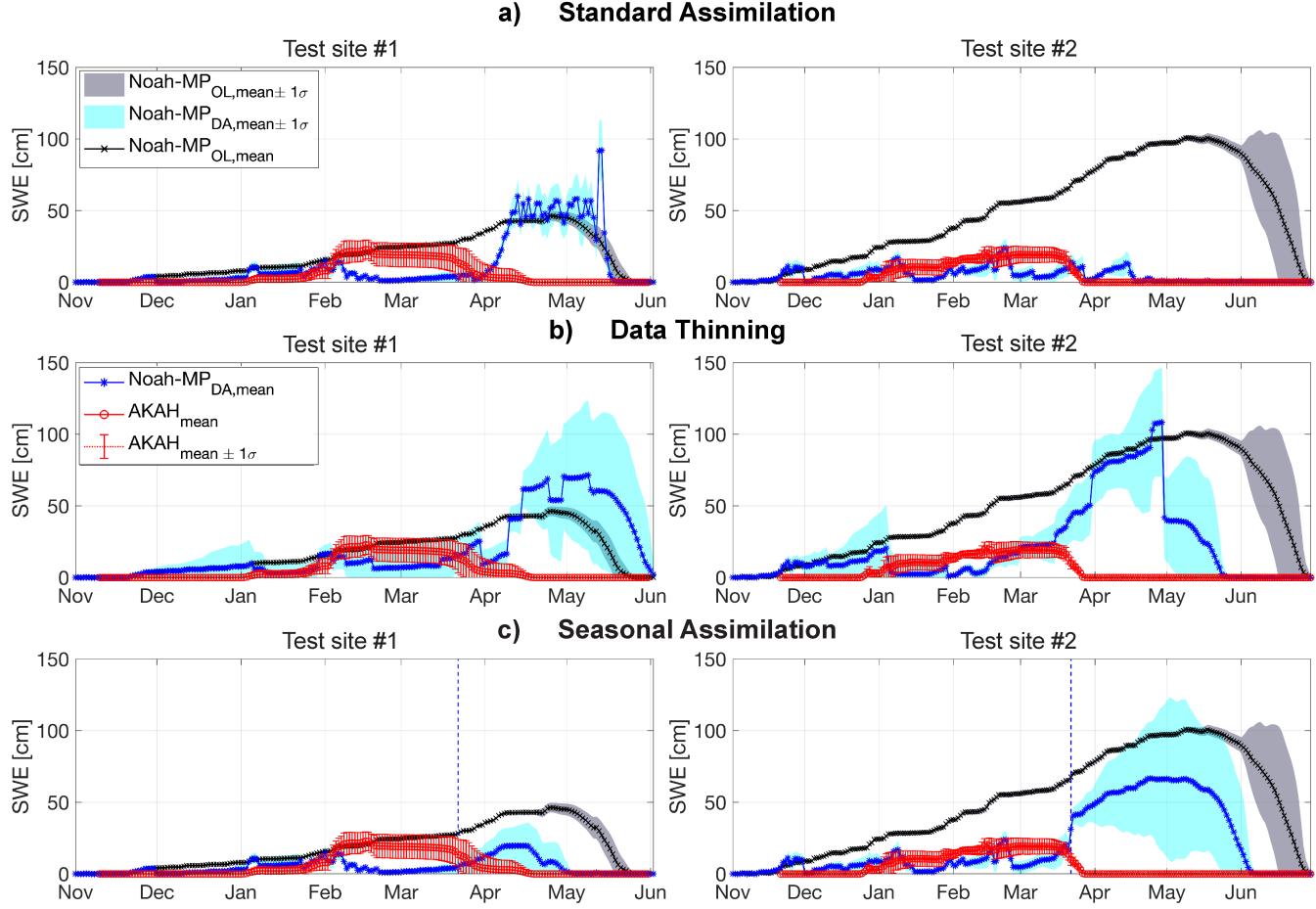


Fig. 7: Comparative timeseries of OL and DA SWE estimates vs. SNOWPACK SWE (modeled using AKAH snow depth measurements) for the 2016-2017 snow season. The dashed lines in part c) locate the date (22 March) when assimilation is disabled for seasonal assimilation. The red solid line represents the mean while the red whiskers represent the standard deviation calculated from SNOWPACK SWE estimates for stations that lie within the Noah-MP grid cell.

659 SWE. Test site #2 shows improved estimates during the accumulation
 660 period, but a large SWE update immediately before
 661 the assimilation is disabled (22 March 2017) considerably
 662 increases the ensemble uncertainty and the ensemble mean
 663 magnitude. For test site #2, the estimates are similar to the
 664 OL here onward as the ensemble is propagated forward in
 665 time without further assimilation.

666 4) *Statistical results:* Table VI contains the domain-
 667 averaged statistics for the three different assimilation runs. The
 668 domain-averaged bias is improved for all of the assimilation
 669 runs as compared to the OL with the highest decrease in
 670 domain-averaged bias obtained via standard assimilation. Data
 671 thinning-based estimates exhibit relatively higher domain-
 672 averaged bias and RMSE as compared to the other assimilation
 673 runs (Table VI). The domain-averaged bias for seasonal assim-
 674 ilation is comparatively on the lower end. The lowest domain-
 675 averaged and domain-median RMSE are exhibited by the
 676 seasonal assimilation approach. It must be noted that these are
 677 domain-averaged values that can be significantly influenced by
 678 large positive or negative bias values at a few locations.

679 Analyzing the computed statistics with respect to land cover
 680 type and elevation, it was noted that, similar to snow depth,

| Statistic [cm] | Open Loop | Standard Assimilation | Data Thinning | Seasonal Assimilation |
|----------------------|-----------|-----------------------|---------------|-----------------------|
| Mean Bias | 24.2 | 14.2 | 20.4 | 14.3 |
| Median Bias | 19.6 | 8.7 | 13.7 | 9.4 |
| Mean RMSE | 34.1 | 33.6 | 37.0 | 29.2 |
| Median RMSE | 27.2 | 24.2 | 29.6 | 20.4 |
| Mean Unbiased RMSE | 22.8 | 27.6 | 28.5 | 23.0 |
| Median Unbiased RMSE | 19.8 | 22.8 | 24.4 | 17.5 |

TABLE VI: Domain-averaged and domain-median bias and RMSE of OL and DA SWE estimates as compared to the SNOWPACK SWE values for the 2016-17 snow season. All values are in units of centimeter.

| Run Type | SWE | | | |
|-----------------------|-----------------------------|----------------|---------------|------------|
| | Elevation of Noah-MP pixels | | | |
| | Mean Bias [cm] | Mean RMSE [cm] | ≤ 4000 m | > 4000 m |
| Open Loop | 30.5 | 14.5 | 40.3 | 24.6 |
| Standard Assimilation | 15.5 | 12.3 | 35.4 | 30.8 |
| Data Thinning | 24.0 | 15.0 | 40.7 | 31.3 |
| Seasonal Assimilation | 15.9 | 11.7 | 30.6 | 27.1 |

TABLE VII: Influence of elevation on ΔT_b assimilation performance. The number of pixels with elevation ≤ 4000 m = 23 whereas the number of pixels with elevation > 4000 m = 15.

the average bias in SWE estimates for pixels categorized as barren land cover was relatively lower for standard and seasonal assimilation runs (11.6 cm and 9.0 cm respectively) as compared to the OL and data thinning runs (25.0 cm and 23.6 cm respectively). Correlations calculated between pixel elevations and statistics (bias and RMSE) were; i) all negative (i.e., as elevation increases the SWE estimates improve), ii) $|R| < 0.5$ for all the DA runs, and iii) equal to -0.5 for the OL. Table VII presents the influence of assimilation on statistics calculated for pixels within different elevation ranges. For pixels at elevation ≤ 4000 m, standard and seasonal assimilation show relatively lower mean bias and RMSE as compared to the OL. For elevation > 4000 m, where deep snow is expected, the OL exhibits a lower mean RMSE than the assimilation runs.

C. Snow accumulation period

Figs. 6 and 7 highlighted that the DA estimates performed much better during the snow accumulation period as compared to the ablation period. The improved performance is due to the relatively higher presence of snow mass-relevant information and the reduction of background noise (i.e., information related to features other than snow mass) in the AMSR2 ΔT_b signal during the snow accumulation period. Figs. 8 and 9 show the maps of snow depth and SWE statistics, respectively, computed for the snow accumulation months only (Nov-Feb). The standard assimilation run is used for both the snow depth and the SWE comparison.

The domain-averaged bias and RMSE for both snow depth and SWE for the OL and the DA are visibly reduced as compared to the complete snow season statistics, presented in Tables IV and VI. This is due to the temporal lag in the snowpack development exhibited by the OL and the DA runs as compared to the AKAH measurements, i.e., the OL and DA simulation peak value occurs after February thus the snow depth and SWE magnitudes of all the estimates are much lower resulting in a smaller bias and RMSE magnitude. The DA snow depth estimates (Fig. 8) exhibit reduced domain-averaged bias and RMSE values as compared to the OL. The Noah-MP_{OL} domain-averaged bias is reduced by 63% through

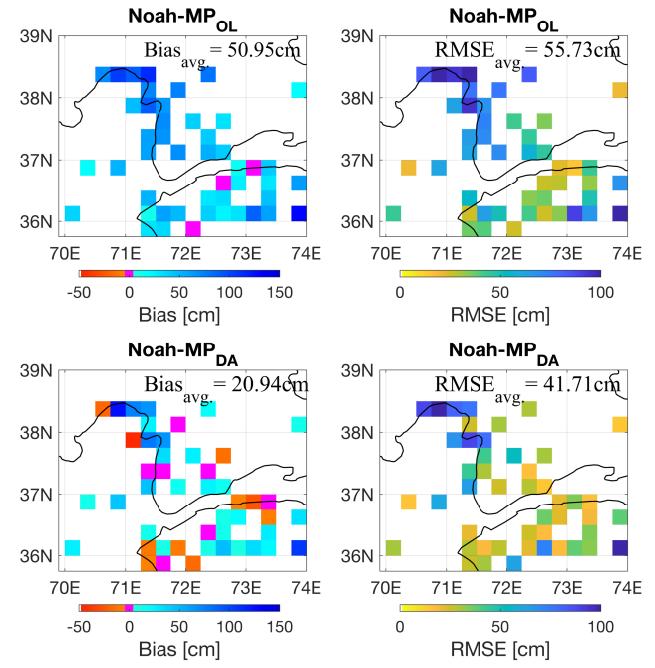


Fig. 8: OL and DA (standard assimilation) maps of bias and RMSE for snow depth estimates during the snow accumulation months (Nov-Feb), 2016-17.

ΔT_b assimilation. The snow depth absolute bias and RMSE were reduced at 47 and 42 (out of 55 total) comparison cells, respectively. Fig. 9 shows a similar reduction in DA SWE bias and RMSE. The OL and DA RMSE maps show similar domain-averaged RMSE magnitudes. The absolute bias and RMSE for the SWE estimates were reduced in magnitude at 29 and 22 (out of 38 total) comparison cells, respectively, as a result of ΔT_b assimilation when considering only the snow accumulation period.

VI. DISCUSSION

According to Tables IV and VI, daily assimilation performed better than incremental-day (data thinning) assimilation as both standard and seasonal assimilation have lower domain-averaged mean and domain-averaged median bias and RMSE as compared to the data thinning assimilation run. Data thinning was performed in an effort to extract snow mass-related information from the ΔT_b signal while reducing the import of high frequency noise and snow mass-irrelevant information into the updated timeseries. However, from Figs. 6b and 7b it is apparent that data thinning resulted in increased uncertainty within the ensemble and, in general, did not serve the intended goal. For seasonal assimilation, we used a first-order approach to identify wet snowpack conditions. Instead of relying on rainfall data, utilization of a more sophisticated approach may yield different results. Meanwhile, it is observed that the standard daily ΔT_b assimilation did reduce the bias and RMSE (as compared to the OL), especially during the snow accumulation months (Nov-Feb). The relatively better results observed during the (dry) snow accumulation season are expected. Several studies have analyzed the differences in

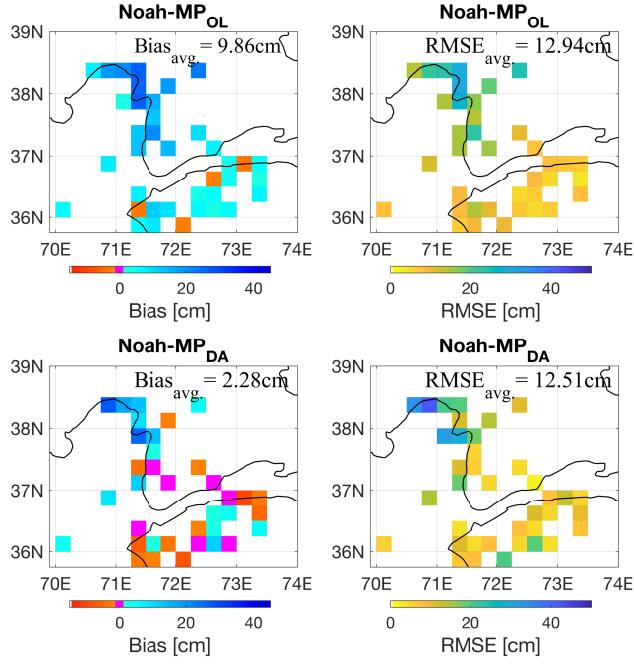


Fig. 9: OL and DA (standard assimilation) maps of bias and RMSE for SWE estimates during the snow accumulation months (Nov-Feb), 2016-17.

750 the relationship between SWE/SD and T_b for dry versus wet
 751 snow conditions [5], [50], [54]. Based on the conclusions of
 752 these studies, it is expected that the effectiveness of extracting
 753 SWE-relevant information from ΔT_b observations during the
 754 snow ablation period would be limited.

755 The results detailed in Section-V indicate the presence of a
 756 general positive bias for all SWE estimates. The positive bias
 757 highlights over-prediction of the OL and DA snow depth and
 758 SWE estimates in the evaluated sub-domain (AKAH domain).
 759 One reason behind the errors in SD and SWE estimates is
 760 the bias in the boundary conditions (i.e., MERRA2). The
 761 Noah-MP land surface model was used to estimate SD and
 762 SWE using MERRA2 boundary conditions (including pre-
 763 cipitation). Through previous analysis, it was observed that
 764 in the complex, high-elevation terrain of HMA, MERRA2
 765 exhibits certain biases [55]. High precipitation magnitudes are
 766 observed during the winter season and a lag is present in
 767 the onset of melt. As a result, the model predicts higher SD
 768 and SWE magnitudes for the snowpack, which completely
 769 melts at a later date as compared to the in situ data. A
 770 future trajectory for this study could be the replication of
 771 the described experiments using alternative model boundary
 772 conditions. Another possible cause of error is the Noah-MP
 773 land surface model's formulation of snow albedo– snow albedo
 774 influences the development and melting of the snowpack.
 775 Kumar et al. [56] studied the spectral components of albedo
 776 estimated by Noah-MP and concluded that errors in the visible
 777 albedo components affected the reflective radiative fluxes,
 778 and hence, the subsequent development and melting of the
 779 snowpack.

780 The general, positive bias could also be due to the elevation

781 difference between the AKAH stations and the Noah-MP
 782 grid cells. The Noah-MP grid cells are generally at a higher
 783 elevation as compared to the corresponding AKAH stations,
 784 and therefore, the snowpack peak SD/SWE and total meltout
 785 in Noah-MP occur at a later date. It should also be stated
 786 that the comparisons detailed above are an evaluation, not a
 787 validation, of the OL and the DA results as: i) differences in
 788 the spatial scales of the in situ measurements versus the Noah-
 789 MP output can give rise to representativeness error, and ii) the
 790 evaluation SWE data is also modeled, although it is predicated
 791 on the in situ AKAH snow depth measurements.

792 The results included in Section-V are computed by com-
 793 paring the OL and DA estimates with the AKAH mea-
 794 surements. These measurements were taken at stations located
 795 in the northwestern part of HMA. Previous studies [4], [21]
 796 have established the presence of different hydrologic regimes
 797 operating within different parts of HMA. Therefore, the results
 798 presented here and the conclusions drawn from them are
 799 applicable primarily to the northwestern part of HMA.

800 A limiting feature in the assimilation framework presented
 801 here is the SVM-based observation operator. It limits the
 802 applicability of the assimilation framework at certain instances
 803 in time, especially during the ablation season, when the
 804 sensitivity of trained SVMs to input SWE is reduced [42].
 805 In addition, information within the AMSR2 ΔT_b observa-
 806 tions related to physical features not related to snow mass (and
 807 which subsequently acts as noise in this framework) is also
 808 transferred to the trained SVMs and can result in erroneous
 809 ΔT_b training and prediction. The ill-posed nature of ΔT_b
 810 translation to SWE in the presence of wet snowpacks is
 811 further heightened when attempting this conversion in complex
 812 terrain.

VII. CONCLUSION

813 In this study, a PMW ΔT_b assimilation framework was
 814 utilized to improve snow estimates over high mountain Asia.
 815 Well-trained SVMs served as the observation operators. Snow
 816 depth and SWE modeled via SNOWPACK based on boundary
 817 conditions specified by in situ snow depth measurements were
 818 used during evaluation in order to asses the accuracy of the
 819 Noah-MP model only (OL) snow estimates versus the ΔT_b
 820 assimilated (DA) estimates. The computed statistics highlight
 821 the improvements in domain-averaged performance of the DA
 822 estimates. Absolute bias in SWE estimates was improved at
 823 74% while RMSE was reduced at 68% of the total comparative
 824 pixels through standard assimilation. Comparing the bias and
 825 RMSE results, it can be stated that assimilation proved more
 826 effective in reducing bias than RMSE.

827 SVM training is an important component of the outlined
 828 framework and it is thus necessary that the SVM training
 829 (input and target) data be analyzed prior to the training process.
 830 The ill-posed nature of the ΔT_b to SWE conversion problem
 831 is partially responsible for the degradation of the estimation
 832 accuracy at particular instances in space and time, especially
 833 during the ablation period when the AMSR2 ΔT_b observa-
 834 tions contain considerable amount of information not relevant to
 835 snow mass thus reducing the relevant information content

837 in the PMW signal. The relatively improved performance of
838 the described framework during the (dry) snow accumulation
839 period and weak performance during the (wet) snow ablation
840 period is expected considering the results of relevant previous
841 studies [5], [50].

842 The experimental results detailed above show that the
843 AMSR2 passive microwave brightness temperatures do add
844 utility to modeled SWE estimates in complex terrain, specifically
845 during the dry snow accumulation months. The coarse
846 PMW ΔT_b observations can be used in areas where finer
847 resolution data does not exist in order to achieve improvements
848 in snow depth and SWE estimation. This study attempts to
849 fill the gap in our knowledge regarding consistent snow mass
850 estimation in HMA, particularly in the northwestern sub-
851 region, through the use of PMW ΔT_b . Although the utilization
852 of PMW for accurate snow estimation in complex terrain is
853 dependent on a multitude of factors, it does exhibit certain
854 utility for improving snow estimation in parts of HMA. One
855 potential path forward is the development and assimilation of
856 physically-enhanced brightness temperature combinations as
857 compared to the simple ΔT_b combinations assimilated in this
858 study. An example would be the utilization of an approach
859 similar to that described by Takala et al. [57] who used a
860 forest factor to scale the ΔT_b magnitude. Another potential
861 strategy could be based on using a cost-function to control
862 the magnitude of SWE update during the wet ablation season
863 using some form of a variational assimilation approach.

864 APPENDIX A 865 SUPPORT VECTOR MACHINE REGRESSION THEORY

866 The Vapnik-Chervonenkis theory [39] forms the basis of
867 SVM regression. In ε - SV regression [58], the objective is
868 to find a function $f(x)$ that has, at most, ε deviations from
869 the training targets, y_i . That is, ε defines the value of the
870 permissible error. A linear form of such an objective function
871 is:

$$f(x) = \langle w, x \rangle + b \quad \text{such that } b \in \mathbb{R} \quad (6)$$

872 where $\langle \cdot, \cdot \rangle$ is the dot product in X (X is the input pattern
873 space and contains the vector x), w is a vector of weights,
874 and \mathbb{R} represents the real number space. This problem can be
875 formulated as an optimization problem [40] as:

$$\begin{aligned} & \text{minimize} && \frac{1}{2} \|w\|^2 \\ & \text{subject to} && \begin{cases} y_i - \langle w, x \rangle - b \leq \varepsilon \\ \langle w, x \rangle + b - y_i \leq \varepsilon \end{cases} \end{aligned} \quad (7)$$

876 where $\|\cdot\|$ represents the Euclidean norm.

877 A non-linear version of this objective function uses a kernel
878 function to map the input data into a higher dimensional
879 feature space where the data displays a linear relationship.
880 The radial basis function (RBF) kernel was used in this study.
881 The RBF kernel has one parameter γ which describes its
882 bandwidth.

883 The SVM algorithm was implemented using the LIBSVM
884 library provided by National Taiwan University [59]. The
885 ε - SV regression requires user-provided values for three
886 parameters: *i*) C , *ii*) ε , and *iii*) γ . C is a penalty parameter

877 and is set as the range of the training targets (y_i) in this study. ε
878 and γ were selected using a two-phase cross-validation method
879 [41], [42]. A separate SVM was trained for each grid cell for
880 each fortnight. Each fortnightly SVM was trained using data
881 from the relevant fortnight as well as two weeks prior to and
882 two weeks after the fortnight under consideration in order to
883 improve temporal continuity from one fortnight to the next.
884 Thus, each SVM was trained using a six-week input dataset
885 and a total of 26 SVMs were produced for each year at each
886 location in space.

887 APPENDIX B 888 STATISTICAL FORMULA

889 The following formulas were used to calculate the bias and
890 RMSE, respectively:

$$891 Bias = \sum_{t=1}^T (y_{\text{simulated}} - y_{\text{observed}}) \quad (8)$$

$$892 RMSE = \sqrt{\frac{\sum_{t=1}^T (y_{\text{simulated}} - y_{\text{observed}})^2}{T}} \quad (9)$$

893 where $y_{\text{simulated}}$ equals the OL/DA snow depth or SWE esti-
894 mate (ensemble mean), y_{observed} is the AKAH snow depth or
895 SNOWPACK SWE, and T is the total number of data instances
896 in time at a given location in space.

897 APPENDIX C 898 SNOWPACK

899 For a more detailed description of the SNOWPACK model
900 runs please see Bair et al. [60] such that only a summary is
901 provided here. SNOWPACK v3.5 was run in research mode
902 at a 15 minute time step with hourly outputs for each of the
903 AKAH stations. Hourly forcings were computed by combin-
904 ing temporally interpolated snow depth from the AKAH in
905 situ measurements with air temperature, incoming shortwave,
906 reflected shortwave, incoming longwave, wind speed, and rel-
907 ative humidity. Radiative forcings were obtained from CERES
908 Ed 4a [49] whereas all the other forcings were collected
909 from GLDAS-2 [48]. These inputs were then downscaled
910 spatially using ParBal [61]. SNOWPACK was only run for
911 periods when measurements from the AKAH stations were
912 available, i.e., Nov/Dec to Apr/May, depending on the year.
913 Grid cells were assumed to be level, hence, forcings without
914 terrain correction were applied except for shading effects
915 when the Sun was below the local horizon [62]. The wind
916 direction, which is not available in GLDAS-2, was fixed as the
917 mean value from the daily AKAH instantaneous values. The
918 ground temperature was set as the daily minimum of the air
919 temperature or -1.5°C when snow cover was present. Changes
920 to default parameters that affected model output are provided
921 in Table A2 of Bair et al. [60].

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925

DATA STATEMENT

926 The source code for NASA Land Information System
927 is available on GitHub (<https://github.com/NASA-LIS/LISF.git>). The code for SNOWPACK is accessible
928 at <https://models.slf.ch/p/snowpack/>. The GLDAS-2
929 (<https://doi.org/10.5067/L0JGCNVBNRAX>, [48]) and
930 MERRA-2 (<https://doi.org/10.5067/VJAFPLIICSV>, [27])
931 forcings are accessible at <https://disc.gsfc.nasa.gov/>. Due to
932 the sensitive geographical location of the study domain, the
933 snow depth measurements used in this study are not publicly
934 available. Requests for the dataset should be made through
935 the Aga Khan Agency for Habitat (<https://www.akdn.org>).

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1162

1163

1164 **Jawairia A. Ahmad** received her M.S. degree in
1165 Civil Engineering from the Department of Civil and
1166 Environmental Engineering, University of Maryland,
1167 College Park, USA, where she is currently pursuing
1168 a Ph.D. Her doctoral dissertation is focused on
1169 improving terrestrial water budget estimation across
1170 high mountain Asia and the adjoining region. Her
1171 research interests include the utilization of machine
1172 learning and data assimilation in Earth science.

1173

1174 **Barton A. Forman** received a B.S. (*cum laude*)
1175 degree in civil engineering from the University of
1176 Virginia, Charlottesville, VA, a M.S. degree in civil
1177 and environmental engineering from the University
1178 of California at Berkeley, Berkeley, CA, and a
1179 Ph.D. degree in civil engineering from the University
1180 of California at Los Angeles, Los Angeles, CA.
1181 Currently, he is an Associate Professor with the
1182 Department of Civil and Environmental Engineering,
1183 University of Maryland, College Park, MD. His
1184 research interests include estimation of snowpack
1185 using space-based measurements of the Earth's gravitational field as well as
1186 high-performance computing applications related to terrestrial hydrology.

1187 **Edward (Ned) H. Bair** received his B.A. in
1188 economics (magna cum laude) from Bowdoin College
1189 in 2003 and his Ph.D. in Environmental Science
1190 and Management in 2011 from the University of
1191 California, Santa Barbara. He has been a member
1192 of the research faculty at UC Santa Barbara since
1193 2011. He uses remote sensing and field techniques
1194 to study the snowpack. He specializes in snow
1195 mapping, energy balance modeling, and avalanche
1196 formation in montane regions. His work spans a
1197 range of scales, from a few meters at the plot scale
1198 to thousands of square kilometers at the basin and mountain range scale. He
1199 has over 50 publications on snow hydrology and snow avalanches. He has
1200 worked for the US Army Corps of Engineers as a consultant. Dr. Bair is
1201 a member of the American Geophysical Union and a professional member
1202 of the American Avalanche Association and its Research Chair. In 2015, he
1203 received the Best Oral Paper Award from the Western Snow Conference.

1204 **Sujay V. Kumar** received Bachelor of Technology
1205 from the Indian Institute of Technology, Bombay in
1206 Civil Engineering in 1996, and Masters (1998) and a
1207 Ph.D. degree (2002) in Computer Aided Engineering
1208 from North Carolina State University, Raleigh, NC.
1209 He is currently a research physical scientist at the
1210 Hydrological Sciences Lab at the NASA Goddard
1211 Space Flight Center. He is the lead of the NASA
1212 Land Information System (LIS) team, a widely-used
1213 high performance platform for land surface modeling
1214 and data assimilation. His research interests include
1215 land surface modeling, data assimilation, remote sensing, high-performance
1216 computing, and machine learning.

